Tennessee End of Course Assessment Algebra I Form 2

**Reporting Category 2: Number and Operations** 

# **PEARSON**

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# **Algebra I Reference Page**

### Abbreviations for Geometric Formulas

A = area d = diameter r = radius

B =area of base h =height s =length of side

b = base  $\ell = \text{length}$  V = volume

 $C = \text{circumference } P = \text{perimeter} \quad w = \text{width}$ 

### Perimeter (P) and Circumference (C)

Any Polygon: P = sum of side lengths

Rectangle:  $P = 2\ell + 2w$ 

Circle:  $C = 2\pi r$  or  $\pi d$ 

 $\pi \approx$  3.14 or  $\frac{22}{7}$ 

# Plane Figures Area (A) Triangle: $A = \frac{1}{2}bh$ Rectangle: $A = \ell w$ Circle: $A = \pi r^2$ $\pi \approx 3.14 \text{ or } \frac{22}{7}$

Solid Figures		Volume ( <i>V</i> )
Right Rectangular Prism	base	$V = Bh$ or $V = \ell wh$
Cube		$V = s^3$

### Algebraic Formulas and Equations

d = rt distance = rate × time

Distance Formula  $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ 

d =distance between two points

Midpoint Formula:  $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$ 

Slope Formula:  $m = \frac{y_2 - y_1}{x_2 - x_1}$ 

Standard Form of

a Linear Equation: Ax + By = C

Slope-Intercept

Equation: y = mx + b

Point-Slope Equation:  $y - y_1 = m(x - x_1)$ 

Pythagorean

Theorem:  $a^2 + b^2 = c^2$ 



### Quadratics

For  $ax^2 + bx + c = 0$ :  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ 

Discriminant:  $b^2 - 4ac$ 

### **Measurement Conversions**

### LENGTH CAPACITY

1 foot (ft) = 12 inches (in.) 1 cup (c) = 8 fluid ounces

1 yard (yd) = 3 feet (fl oz)

1 gallon (gal) = 4 quarts

### **WEIGHT**

1 pound (lb) = 16 ounces (oz) 1 ton (T) = 2,000 pounds

# CONVERSION BETWEEN CUSTOMARY AND METRIC MEASUREMENT

1 foot = 0.3048 m 1 ounce = 28.35 g 1 inch = 2.54 cm 1 lb = 0.45 kg

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### Introduction to Algebra I

### **Content of tests**

The testing program titled the *Tennessee End of Course Assessment* was established to meet the Tennessee mandate for end of course assessments in Tennessee secondary schools. These tests measure the Tennessee State Performance Indicators. Subject areas covered by the end of course assessments include Mathematics, Language Arts, History, and Science.

### **Test development**

For the *Tennessee End of Course Assessment*, a staff of writers – composed of both teachers and professional test developers experienced in each of the content areas – researched and wrote the items. Professional editors and content specialists carefully reviewed all items and test directions for content and accuracy. To provide a large pool of items for final test selection, the test developers created approximately twice as many items as were needed in the final editions of the tests.

After tryout tests were administered, student responses were analyzed. Professional content editors and researchers carefully reviewed items, their data, and test directions for content, suitability, and accuracy before including particular items and test directions in operational tests.

### **Test administration**

Tennessee End of Course Assessments are given to students as they near the end of courses that are included in the program. Tests may be given midyear for block schedules or at the end of the school year.

This test contains 65 multiple-choice questions.

You will have ample time to read and answer each of the questions. The Algebra I test has been designed to be administered in one session and is not timed. The first 15 minutes are set aside to complete identifying data on the answer sheet.

Calculator use is optional. Sharing calculators during testing is not permitted.

The following types of calculators/devices may **NOT** be used during the test:

- pocket organizers
- electronic writing pads or input devices
- Some examples of prohibited calculators are:
  - o Casio models: CFX-9970G, Algebra FX 2.0
  - o Hewlett-Packard models: HP-40G, HP-49G
  - o Texas Instruments models: TI-89, TI-92, Voyage 200, TI-NSPIRE the CAS version (The non-CAS version of TI-NSPIRE is allowable.)
- calculators that can communicate (transfer data or information) wirelessly with other student calculators/devices
- cell phones, PSPs, and/or iPods
- Students may use any four-function, scientific, or graphing calculator does not have any of the above features. The use of units that have a Computer Algebra System (CAS) is NOT allowed.

## **Tips for Taking the Test**

### Preparing for the test

- Review this Tennessee End of Course Item Sampler for Algebra I carefully and thoroughly.
- Acquire the Tennessee End of Course Practice Test for Algebra I, and take the test several times.
- Become familiar with the correct way to mark answers on the answer sheet. There is a sample answer sheet in this Practice Test.

### Before the test

• Get a good night's sleep. To do your best, you need to be rested.

### **During the test**

- Relax. It is normal to be somewhat nervous before the test. Try to relax and not worry.
- Listen. Listen to and read the test directions carefully. Ask for an explanation of the directions if you do not understand them.
- Plan your time. Do not spend too much time on any one question. If a question seems to take too long, skip it and return to it later. First answer all questions that you are sure about.
- Think. If you are not sure how to answer a question, read it again and try your best to answer the question. Rule out answer choices that you know are incorrect and choose from those that remain.

# **Directions for Using the Item Sampler**

This Item Sampler for Algebra I provides specific information to students and teachers. It contains examples of different item types for each Performance Indicator that may be tested in any given end of course test administration. Performance Indicators have been grouped by Reporting Categories. These Reporting Categories will be used to report information regarding performance on the end of courts test to students, teachers, schools, and systems.

The items in this Item Sampler will not be found in the end of course tests. The number of items in this Item Sampler does not reflect the emphasis of content on the test. In order to identify the emphasis of content, the End of Course Assessment Practice Test for Algebra I should be used. The Practice Test gives a better representation of content emphasis across Reporting Categories and Performance Indicators.

An Answer Key is located in Page 17. Use it to check your answers. Review items that you get wrong.

# **Reporting Category:**

# **Number and Operations**

Numbers 1 through 15

**Performance Indicator:** 3102.2.1 Operate (add, subtract, multiply, divide, simplify, powers) with radicals and radical expressions including radicands involving rational numbers and algebraic expressions.

1.

Simplify  $\sqrt{\frac{100x^2}{4}} - 20x$  for all  $x \ge 0$ .

- **A** -15*x*
- **B** -10x
- C 5x
- O D 25x

**Performance Indicator:** 3102.2.1 Operate (add, subtract, multiply, divide, simplify, powers) with radicals and radical expressions including radicands involving rational numbers and algebraic expressions.

2.

What is the product of  $(2\sqrt{q} + 3\sqrt{r})$  and  $7\sqrt{q}$ , if q and r are positive integers?

- $\bigcirc$  **A**  $9\sqrt{q} + 10\sqrt{qr}$
- **B**  $14\sqrt{q} + 21\sqrt{qr}$
- **C**  $14q + 3\sqrt{r}$
- **D**  $14q + 21\sqrt{qr}$

**Performance Indicator:** 3102.2.1 Operate (add, subtract, multiply, divide, simplify, powers) with radicals and radical expressions including radicands involving rational numbers and algebraic expressions.

(3.

Simplify:  $\frac{12\sqrt{x}}{\sqrt{3}}$ 

- $\bigcirc$  A  $4\sqrt{x}$
- B 36√x
- **C**  $4\sqrt{3x}$
- **D**  $12\sqrt{3x}$

**Performance Indicator:** 3102.2.1 Operate (add, subtract, multiply, divide, simplify, powers) with radicals and radical expressions including radicands involving rational numbers and algebraic expressions.

4.

Simplify:  $\left(\sqrt{3r^2s}\right)^6$ 

- **A** 9r<sup>6</sup>s<sup>3</sup>
- **B** 9r<sup>5</sup>s′
- $\circ$  **C**  $27r^5s^4$
- 0 **D**  $27r^6s^3$

**Performance Indicator:** 3102.2.1 Operate (add, subtract, multiply, divide, simplify, powers) with radicals and radical expressions including radicands involving rational numbers and algebraic expressions.

(5.

Which number when multiplied by the expression  $\sqrt{256x^2}$  gives the product of -4x for all  $x \ge 0$ ?

- **B** -4
- $\circ$  C  $\frac{1}{4}$
- O D 4

Performance Indicator: 3102.2.2 Multiply, divide, and square numbers expressed in scientific notation.

6.

A can of soup weighs 10.5 ounces. If one ounce is about  $2.84 \times 10^{-2}$  kilograms, how much does the can of soup weigh in kilograms?

- $\circ$  **A** 2.982  $\times$  10<sup>-4</sup>
- $\odot$  **B** 2.982  $\times$  10<sup>-3</sup>
- $\circ$  **C** 2.982  $\times$  10<sup>-2</sup>
- $\bigcirc$  **D** 2.982  $\times$  10<sup>-1</sup>

Performance Indicator: 3102.2.2 Multiply, divide, and square numbers expressed in scientific notation.

7.

The table shows the speed of light in meters per second through a vacuum and ice.

Speed of Light

Medium	Speed (meters per second)	
Vacuum	$3.0 \times 10^8$	
Ice	$2.3\times10^{8}$	

To the nearest tenth, how many times faster does light travel in a vacuum than in ice?

- A 0.7
- B 0.8
- C 1.3
- **D** 1.5

Performance Indicator: 3102.2.2 Multiply, divide, and square numbers expressed in scientific notation.

8.

On a particular day, a gas station sells  $3.5\times 10^4$  gallons of gasoline. If 1,750 cars get gas on that day, what is the average number of gallons pumped per car?

- A 20
- **B** 50
- **C** 200
- O **D** 500

Performance Indicator: 3102.2.2 Multiply, divide, and square numbers expressed in scientific notation.

9.

Which expression is equivalent to  $(4.5 \times 10^4)^2$ ?

- $\circ$  **A** 2.025  $\times$  10<sup>5</sup>
- $\odot$  **B** 2.025  $\times$  10<sup>6</sup>
- $\bigcirc \quad \boldsymbol{C} \quad 2.025 \times 10^8$
- $\bigcirc$  **D** 2.025  $\times$  10<sup>9</sup>

Performance Indicator: 3102.2.2 Multiply, divide, and square numbers expressed in scientific notation.

(10.

Simplify:  $(2.3 \times 10^{-6})^2$ 

- $\odot$  **A** 5.29  $\times$  10<sup>-12</sup>
- $\odot$  **B**  $4.6 \times 10^{-12}$
- $\odot$  **C** 5.29  $\times$  10<sup>-4</sup>
- $\odot$  **D**  $4.6 \times 10^{-4}$

**Performance Indicator:** 3102.2.3 Describe and/or order a given set of real numbers including both rational and irrational numbers.

(11.

Which number lies between  $\frac{25}{7}$  and  $\frac{36}{8}$ ?

- $\circ$  A  $\sqrt{10}$
- B  $\sqrt{11}$
- C √17
- **D**  $\sqrt{27}$

**Performance Indicator:** 3102.2.3 Describe and/or order a given set of real numbers including both rational and irrational numbers.

12.

Which list shows the numbers arranged from least to greatest?

- $\bigcirc$  **A** 5.32,  $\frac{4}{5}$ ,  $\sqrt{17}$ ,  $\frac{12}{5}$
- $\bigcirc$  **B**  $\frac{4}{5}$ , 5.32,  $\frac{12}{5}$ ,  $\sqrt{17}$
- $\circ$  **c** 5.32,  $\sqrt{17}$ ,  $\frac{12}{5}$ ,  $\frac{4}{5}$
- $\bigcirc$  **D**  $\frac{4}{5}$ ,  $\frac{12}{5}$ ,  $\sqrt{17}$ , 5.32

**Performance Indicator:** 3102.2.3 Describe and/or order a given set of real numbers including both rational and irrational numbers.

(13.

Which set of numbers is ordered from greatest to least?

- $\bigcirc$  **A**  $\left\{\sqrt{31}, 3.85, \frac{7}{9}, \frac{10}{16}\right\}$
- $\circ$  **B**  $\left\{\frac{10}{16}, \frac{7}{9}, 3.85, \sqrt{31}\right\}$
- $\circ$  **c**  $\left\{\frac{10}{16}, 3.85, \frac{7}{9}, \sqrt{31}\right\}$
- $\bigcirc$  **D**  $\left\{\sqrt{31}, \frac{7}{9}, 3.85, \frac{10}{16}\right\}$

**Performance Indicator:** 3102.2.3 Describe and/or order a given set of real numbers including both rational and irrational numbers.

(14.

Which list shows the numbers ordered from greatest to least?

- $\bigcirc$  **A** 4.36,  $\sqrt{23}$ , 5.108, 5.35
- $\bigcirc$  **B** 5.108, 5.35, 4.36,  $\sqrt{23}$
- $\circ$  **C** 5.35, 5.108,  $\sqrt{23}$ , 4.36
- $\bigcirc$  **D** 4.36, 5.108,  $\sqrt{23}$ , 5.35

# Algebra I Item Sampler

**Performance Indicator:** 3102.2.3 Describe and/or order a given set of real numbers including both rational and irrational numbers.



Which set of numbers is ordered from least to greatest?

- $\bigcirc$  **A**  $\left\{\frac{17}{2}, \sqrt{49}, \frac{26}{4}, \sqrt{22}\right\}$
- $\bigcirc$  **B**  $\left\{\sqrt{22}, \sqrt{49}, \frac{26}{4}, \frac{17}{2}\right\}$
- $\circ$  **c**  $\left\{\frac{17}{2}, \frac{26}{4}, \sqrt{22}, \sqrt{49}\right\}$
- $\bigcirc$  **D**  $\left\{\sqrt{22}, \frac{26}{4}, \sqrt{49}, \frac{17}{2}\right\}$

Reporting Category 2: Number and Operations			
Item Number	Correct Answer	Performance Indicator	
1	A	3102.2.1 Operate (add, subtract, multiply, divide, simplify, powers) with radicals and radical expressions including radicands involving rational numbers and algebraic expressions.	
2	D	3102.2.1 Operate (add, subtract, multiply, divide, simplify, powers) with radicals and radical expressions including radicands involving rational numbers and algebraic expressions.	
3	С	3102.2.1 Operate (add, subtract, multiply, divide, simplify, powers) with radicals and radical expressions including radicands involving rational numbers and algebraic expressions.	
4	D	3102.2.1 Operate (add, subtract, multiply, divide, simplify, powers) with radicals and radical expressions including radicands involving rational numbers and algebraic expressions.	
5	A	3102.2.1 Operate (add, subtract, multiply, divide, simplify, powers) with radicals and radical expressions including radicands involving rational numbers and algebraic expressions.	
6	D	3102.2.2 Multiply, divide, and square numbers expressed in scientific notation.	
7	С	3102.2.2 Multiply, divide, and square numbers expressed in scientific notation.	
8	A	3102.2.2 Multiply, divide, and square numbers expressed in scientific notation.	
9	D	3102.2.2 Multiply, divide, and square numbers expressed in scientific notation.	
10	A	3102.2.2 Multiply, divide, and square numbers expressed in scientific notation.	
11	С	3102.2.3 Describe and/or order a given set of real numbers including both rational and irrational numbers.	
12	D	3102.2.3 Describe and/or order a given set of real numbers including both rational and irrational numbers.	

13	A	3102.2.3 Describe and/or order a given set of real numbers including both rational and irrational numbers.
14	С	3102.2.3 Describe and/or order a given set of real numbers including both rational and irrational numbers.
15	D	3102.2.3 Describe and/or order a given set of real numbers including both rational and irrational numbers.